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# Sliding Mode Control of Biglide Planar Parallel Manipulator

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Keywords: Parallel Manipulators, Nonlinear Control, Lyapunov Stability, Sliding Mode Control.

Abstract:

This work presents the control of a two-degree of freedom parallel manipulator using nonlinear sliding mode approach. The aim is to achieve a robust control for trajectory tracking. The control is based on the inverse dynamic model in the Cartesian space of the parallel manipulator. Kinematic analysis are also discussed. To guarantee the high performance on the tracking control. Biglide robot requires full knowledge on the system's dynamics. In this paper, some important properties of the parallel manipulators are considered to develop a sliding mode controller which can drive the movement tracking error to zero asymptotically. Numerical simulations are completed to show the effectiveness of the approach for a large parameter variations.

#### INTRODUCTION 1

Parallel Robots are closed loop kinematic chain mechanisms. They have several advantages compared to serial link manipulator, such as high accuracy, high stiffness, high payload capability and low moving inertia, etc. Therefore, they attracted a lots of researchers's interests in recent decades (Omran, A and Elshabasy, M. 2010) (Cheng, H., Yiu, Y. K., and Li, Z., 2003). They are widely used in different applications, such as machine tools (Abdellatif, H., Grotjahn, M., and Heimann, B. 2005), industrial high speed applications (Weck, M., Staimer, D. 2002), medical robots, micro robots (Jamwal, P. K., Xie, S. O., Tsoi, Y. H., and Aw, K. C. 2010), humanoid robots and flight simulators by (Gough, V. E. 1956) (Stewart, D. 1965). Despite of their advantages, parallel robots have also some drawbacks, such as limited workspace and complex kinematic issues caused by the presence of multiple closed loop chains and singularities. In this paper, we will discuss the motion control of a planar parallel robot with two degrees of freedom (DOF)(Vermeiren, L., Dequidt, A., Afroun, M., and Guerra, T. M. 2012).

(Cheung, J. W., Hung, Y. S. 2005), (Pierrot, F., Krut, S., Baradat, C., and Nabat, V. 2011) are used These types of robots in the manufacturing industry of electronic products, as pick and place applications.

A dynamical analysis of parallel robot is very

complex because the existence of multiple close-loop chains. In addition, due to uncertainties such as not modeled errors on dynamic parameters, measurement noise and external disturbances. Many researchers worked on the dynamic modeling of parallel robots as in (Khalil, W., Ibrahim, O. 2007), (Staicu, S., Liu, X. J., and Wang, J. 2007) and (Staicu, S. 2009).

The Conventional control methods of parallel manipulators have attracted many researchers in studying their performances. A proportional derivative (PD) controller (Ghorbel, F. H., Chtelat, O., Gunawardana, R., and Longchamp, R. 2000), a nonlinear PD controller (Ouyang, P. R., Zhang, W. J., and Wu, F. X. 2002) and an adaptive switching learning PD control method (Ouyang, P. R., Zhang, W. J., and Gupta, M. M. 2006), (Le, T. D., Kang, H. J., and Suh, Y. S. 2013) were proposed for the motion control of parallel manipulators. It is also noted in (Piltan, F., Rahmdel, S., Mehrara, S., and Bayat, R. 2012) that all of these controllers are simple and easy to implement but they are not robust in presence of uncertainties or when the robot supports different payloads. Some other advanced controllers were proposed, such as the computed torque controller (Vermeiren, L., Dequidt, A., Afroun, M., and Guerra, T. M. 2012), (Yang, Z., Wu, J., and Mei, J. 2007), and the adaptive controller (Zhu, X., Tao, G., Yao, B., and Cao, J. 2009). These approaches are based on a full knowledge dynamic model and require a computational power. However,

it is complicated to obtain a precise dynamic model of the parallel manipulators, due to the aforementioned drawback (Le, T. D., Kang, H. J., and Suh, Y. S. 2013).

In this paper, a new contribution is proposed to control parallel robot in the cartesian space. This approach is based on the inverse dynamic model and sliding mode technics (Vermeiren, L., Dequidt, A., Afroun, M., and Guerra, T. M. 2012). The theory of sliding mode control has been successfully applied to serial manipulators (Slotine, J. J. E., Li, W. 1991), (Sadati, N., Ghadami, R. 2008) and (Zeinali, M., Notash, L. 2010). This approach exhibits the property of robustness for its ability to reject the uncertainties and the external disturbances which satisfy the matching conditions (Castaos, F., Fridman, L. 2006), (AL-Samarraie, S. A. 2013). The advantage of sliding mode is low sensitivity versus parameter variations and disturbances. The design of sliding mode controller consists in two steps: The choice of the sliding variable according to the control objective. While the second is to use a discontinuous control to force  $q = g(P) \tag{4}$ the state trajectories of the system to reach the sliding surface in a finite time and to evolve on it in spite of disturbance.(AL-Samarraie, S. A. 2013), (Utkin, V., Guldner, J., and Shijun, M. 1999). Sliding mode control has been used for several applications such as Underwater vehicles (Sankaranarayanan, V., Mahindrakar, A. D. 2009), Active vehicle suspensions (Geravand, M., Aghakhani, N. 2010), Magnetic levitation (Lin, F. J., Chen, S. Y., and Shyu, K. K. 2009), DC-DC converters (Tan, S. C., Lai, Y. M., and Tse, C. K. 2008) and photovoltaic solar in (Khiari, B., Sellami, A., Andoulsi, R., and Mami, A. 2012).

This paper is organized as follows. In Section2, the dynamic model of 2-DOF parallel manipulator is formulated in the Cartesian space. In Section3, sliding mode controller is developed and applied to the inverse dynamic model of robot in Cartesian space the Section4, presents simulation results of the proposed controller. Finally, some conclusions are presented in the closing section.

#### DYNAMICS MODELING OF 2 BIGLIDE PARALLEL ROBOT

#### 2.1 **Kinematic and Geometric Analysis**

For the geometric and kinematics modeling of a Biglide parallel manipulator, the following conventions are used according to (Vermeiren, L., Dequidt, A., Afroun, M., and Guerra, T. M. 2012). The manipulator provides 2DOF of translation on the XY plane, the positioning of end effector is represented by operational variables (x, y) driven by two prismatic active joints  $(q_1, q_2)$  in the same X axis.

The operational vector is then written as follow:

$$P = \begin{bmatrix} x & y \end{bmatrix}^T \tag{1}$$

The generalized joint variable vector is:

$$q = [q_1 \quad q_2]^T \tag{2}$$

The mechanism has two constant length struts with moveable foot points Figure 1. Both struts have the same lengtha. The relationship between both coordinate vectors is written with kinematic loopclosure constraints Figure 1:

$$\Phi(P,q) = 0, \Phi(P,q) = \begin{pmatrix} (x-q_1)^2 + y^2 - a^2 \\ (q_2 - x)^2 + y^2 - a^2 \end{pmatrix}. \quad (3)$$

The Inverse geometric model (IGM) formula is given by:

$$q = g(P) \tag{4}$$

$$g(P) \equiv \begin{pmatrix} x - C(y) \\ x + C(y) \end{pmatrix}, C(y) \equiv \sqrt{a^2 - y^2}$$
 (5)

The direct geometric model (DGM) can be derived from (4):

$$P = g^{-1}(q) \tag{6}$$

with

$$g^{-1}(q) = \left(\frac{\frac{q_1 + q_2}{2}}{\sqrt{a^2 - \frac{(q_1 + q_2)^2}{4}}}\right) \tag{7}$$

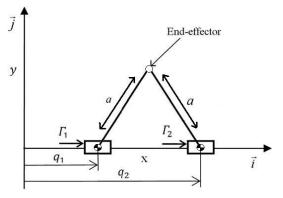


Figure 1: kinematic schemes of Biglide robot.

The relation between the joint space and the operational space is conveniently described by two Jacobian matrices  $J_p(P,q)$  and  $J_q(P,q)$  is given as:

$$J_p(P,q)\dot{P} = J_q(P,q)\dot{q} \tag{8}$$

The parallel singularities occur when the Jacobian

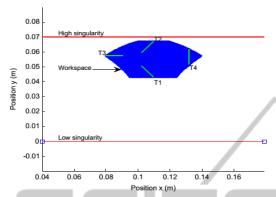


Figure 2: Workspace and trajectories: (T1) Low trajectory, (T2) High trajectory, (T3) Left trajectory, and (T4) Right trajectory.

matrix  $J_p$  is rank deficient. The Biglide has two parallel singularities: (Vermeiren, L., Dequidt, A., Afroun, M., and Guerra, T. M. 2012)

- High singularity:  $q_1 = q_2 = x$ , the struts are superposed and y = 0.07, Figure 2.
- Low singularity: y = 0, the struts are aligned, Figure 2

The kinematic relationship between end-effector velocities and joint velocities is computed by differentiating (3) with respect to time:

$$J_p(P,q)\dot{P} = J_q(P,q)\dot{q} \text{ with } J_p(P,q) = \begin{bmatrix} x - q_1 & y \\ x - q_2 & y \end{bmatrix}$$

$$J_p(P,q) = \begin{bmatrix} x - q_1 & 0 \\ 0 & x - q_2 \end{bmatrix} \tag{9}$$

# 2.2 Dynamic Model

The dynamics equations of the Biglide in operational space are given as follows (Vermeiren, L., Dequidt, A., Afroun, M., and Guerra, T. M. 2012):

$$\Gamma = M(P)\ddot{P} + N(P,\dot{P}) \tag{10}$$

with

 $P = \begin{bmatrix} x & y \end{bmatrix}^T$ , M(P) is the inertial matrix given as follow:

$$M(P) = \begin{pmatrix} m_1 + \frac{1}{2}(m - \lambda_1 + \lambda_2) & f_1(P) \\ m_2 + \frac{1}{2}(m - \lambda_2 + \lambda_1) & f_2(P) \end{pmatrix}$$
(11) with

$$\lambda_{1,2} = ms_{1,2}/a$$

$$f_1(P) = [(2m_1 - 3\lambda_1 - \lambda_2)y^2 + mC(y)^2 + J_1 + J_2]/(2C(y) \times y)$$
  

$$f_2(P) = -[(2m_2 - 3\lambda_2 - \lambda_1)y^2 + mC(y)^2 + J_1 + J_2]/(2C(y) \times y)$$

$$N(P, \dot{P}) = N(y, \dot{y}) + p(y)$$

 $N(y,\dot{y})$  is a coriolis / centripetal matrix can be written as:

$$R(y, \dot{y}) = \begin{bmatrix} r_{11} & r_{12} \\ r_{21} & r_{22} \end{bmatrix}$$
 (12)

$$\begin{cases} r_{11} = r_{12} = 0 \\ r_{12} = -[(2m_1 - 3\lambda_1 - \lambda_2)y^2 + (2m_1 - 3\lambda_1 - \lambda_2) \\ C(y)^2 + J_1 + J_2]\dot{y}/(2C(y)^3 \\ r_{22} = [(2m_2 - 3\lambda_2 - \lambda_1)y^2 + (2m_2 - 3\lambda_2 - \lambda_1) \\ C(y)^2 + J_1 + J_2]\dot{y}/(2C(y)^3 \end{cases}$$

p(y) is a vector containing gravity torques can be written as:

$$p(y) = \begin{pmatrix} (gC(y)(m + \lambda_1 + \lambda_2))/2y \\ (-gC(y)(m + \lambda_1 + \lambda_2))/2y \end{pmatrix}$$
(13)

# 3 CONTROLLER DESIGN

In this section the control law based on sliding mode approach is applied on the inverse dynamic model in operational space of the Biglide.

From equation (10), the direct dynamic model in operational space is given as fallow:

$$\ddot{P} = M(P)^{-1} [\Gamma - N(P, \dot{P})] \tag{14}$$

with

 $P = \begin{bmatrix} x & y \end{bmatrix}^T$  is x and y vector positions of the endeffector.  $\Gamma = \begin{bmatrix} \Gamma_1 & \Gamma_2 \end{bmatrix}^T$  is torque vector.

## 3.1 Sliding Mode Control

The tracking control problem in operational space is to find a control law such that given a desired trajectory  $P_{des}$ , and the tracking error  $e_i$  is go to zero asymptotically.

where

$$e_i = P_{mes} - P_{des}, i = (1, 2).$$
 (15)

with

 $P_{mes} = \begin{bmatrix} x_{mes} & y_{mes} \end{bmatrix}^T$  is measure position vector of the end-effector.

 $P_{des} = \begin{bmatrix} x_{des} & y_{des} \end{bmatrix}^T$  is desired position vector of the end-effector.

The relative degree of the system from (8) r = 2, the sliding surface selected in our work is given by:

$$S = \dot{e} + \lambda e \tag{16}$$

where  $\lambda$  is 2 \* 2 diagonal positive definite matrix.

Consider the following Lyapunov function candidate

$$V = \frac{1}{2}S^T S \tag{17}$$

Time derivative of (11) will lead to

$$\dot{V} = S^T \dot{S} \tag{18}$$

In which the term  $\dot{S}$  is given by

$$\dot{S} = \lambda \dot{e} + P_{mes}^{"} - P_{des}^{"} \tag{19}$$

where

$$\ddot{P}_{mes} = M(P)^{-1} [\Gamma - N(P, \dot{P})]$$
 (20)

with

 $\ddot{P}_{mes} = \begin{bmatrix} \ddot{x}_{mes} & \ddot{y}_{mes} \end{bmatrix}^T$  is measure acceleration vector of the end-effector.

Taking (20) for  $\ddot{P}_m$  and substituting in (19) results in

$$\dot{S} = \lambda \dot{e} - \ddot{P}_{des} + M(P)^{-1} [\Gamma - N(P, \dot{P})]$$
 (21)  
From equation (20) we can write equation (18) as

$$\dot{V} = S^{T} [\lambda \dot{e} - \ddot{P}_{des} + M(P)^{-1} [\Gamma - N(P, \dot{P})]]$$
 (22)

From Lyapunov stability theory we know that the system reaches S=0 in finite time of the above Lyapunov function and  $\dot{V}=S\dot{S}<0$  Defining the control signal as

$$\Gamma = \hat{\Gamma} - MKsgn(S) \tag{23}$$

with

$$\Gamma = \begin{bmatrix} \Gamma_1 & \Gamma_2 \end{bmatrix}^T$$

and  $\hat{\Gamma}$  is defined as

$$\hat{\Gamma} = [M(P)(P_{des} - \lambda \dot{e}) + N(P, \dot{P})] \tag{24}$$

will cause

$$\dot{S} = -Ksign(S) \tag{25}$$

with  $K \in \mathbb{R}^{2*1}$  is the gain and sign(S) is switching function.

Hence, according to the Lyapunov theory the control law (22) will result in a stable closed loop system. In practice, the control law (22) cannot be used because of containing the term sign(S) which results in high frequency oscillations, called chattering, and it is replaced by a continuous approximation. Chattering may be reduced by using a high saturation function. We define control law and tracking as

$$\Gamma = \hat{\Gamma} - MKsat(S) \tag{26}$$

where sat(S) is a saturation function and can be defined as follow

$$sat\left(S(t)\right) = \begin{cases} \frac{S(t)}{\|S(t)\|} & si \quad S(t) \ge \delta \\ \frac{S(t)}{\|S(t) + \delta\|} & si \quad S(t) < \delta \end{cases}$$

which provide a very smooth control action.

# 4 SIMULATION RESULTS

The Biglide manipulator is tested in simulation in order to validate sliding mode controller. The reference trajectory tracking (a 5th order polynomial interpolation), The numerical parameters simulation of dynamic model are defined from Table I in Appendix.

- CTC: Computed Torque Control (Vermeiren, L., Dequidt, A., Afroun, M., and Guerra, T. M. 2012);
- SMC: sliding mode Control, Eqs. (22);

The model of the parallel robot used for numerical simulation includes structured and unstructured uncertainties. The structured uncertainty is considered for a variation of the end effector mass corresponding to  $\Delta m = 0.816kg$  of course no uncertainty corresponds to  $\Delta m = 0$ .

Simulation has been performed in-order to examine the effectiveness of proposed controller design.

#### 4.1 Discussion of Simulation Results

The simulation results of CTC controller (Vermeiren, L., Dequidt, A., Afroun, M., and Guerra, T. M. 2012) and sliding mode controller are presented in Figs. 2 and 4 for the trajectories T1 (near to workspace low boundary) and Figs. 3 and 5 for T2 (near to workspace high boundary), for each figure trajectories, parts (a) and (b) present the set Point and the response along x and y axes and parts (c) and (d) present the control input of both actuators.

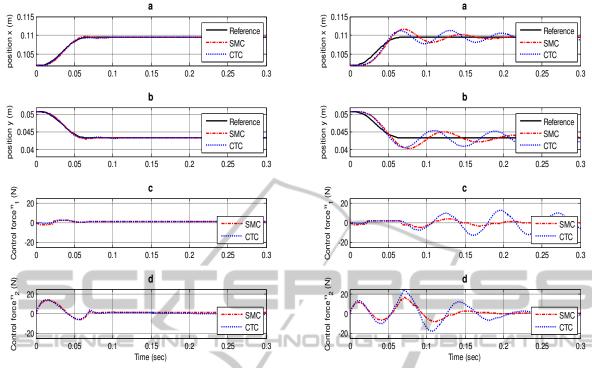


Figure 3: Control schemes for low trajectory (T1) and  $\Delta m = 0$ .

Figure 5: Control schemes for low trajectory (T1) and  $\Delta m = 0.816$ .

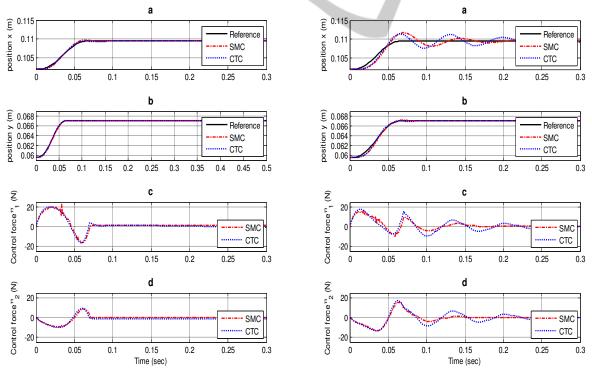


Figure 4: Control schemes for high trajectory (T2) and  $\Delta m = 0$ .

Figure 6: Control schemes for high trajectory (T2) and  $\Delta m = 0.816$ .

Note also that Figs. 2 and 3 are without mass variation  $\Delta m = 0$  Where as Figs. 4 and 5 uses a  $\Delta m = 0.816 Kg$ . The mass variation is used to check the robustness of these controllers. In the former case, $\Delta m = 0$ , going from the best to the worst; The sliding mode Controller and CTC controller shows a good capability of response. Based on Figure 4 and 5; by comparing response trajectory with mass variation of platform  $\Delta m = 0.816 Kg$  the sliding mode control presents the good results according to structured uncertainties (parametric variation), and for the CTC which is presents some important overshoot with some oscillation in trajectory response. In order to quantify the behavior of the controllers CTC and sliding mode controller some well-known criteria are computed for 4 trajectories T1, T2, T3 and T4 in the work space (Vermeiren, L., Dequidt, A., Afroun, M., and Guerra, T. M. 2012). The criteria is computed over a time simulation of  $T = 2_s$  using the error vector, and the control force input vector.

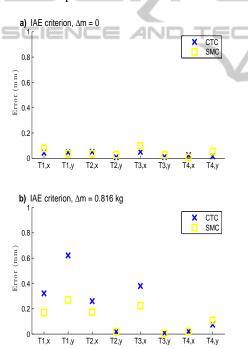
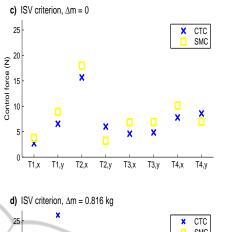


Figure 7: (a)-(c) Performance criteria (position error and control force) computed for all displacements (T1&T4) trajectories along x and y axes), $\Delta m = 0$ .

From the Fig. 6 and 7 for all trajectories the sliding mode control shows a good tracking performance for all displacement (T1, T2, T3, and T4). The results confirm previous observations. with mass variations, the sliding mode is more robust and sensitive to each parametric change compared with CTC controller.



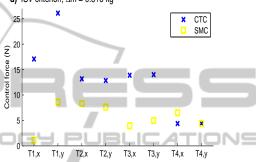


Figure 8: (b)-(d) Performance criteria (position error and control force) computed for all displacements (T1&T4) trajectories along x and y axes), $\Delta m = 0.816$ .

### 5 CONCLUSION

This paper, present different results of a nonlinear control approach applied to a planar 2DOF parallel manipulator Biglide type. Using sliding mode control approach to achieve a best performance and robust control for trajectory tracking, the control is based on the inverse dynamic model in the Cartesian space of the parallel manipulator. The sliding mode is employed successfully for the regulation and tracking of a multi input multi output planer parallel robot in presence of nonlinearities. Stability analysis based on Lyapunov theory is performed to guarantee global, asymptotic and exponential convergence.

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## **APPENDIX**

Numerical simulations include a model with structured and unstructured uncertainties based on the nominal model used to design the controller. Unmodeled dynamics such as elastic joints (Vermeiren, L., Dequidt, A., Afroun, M., and Guerra, T. M. 2012) between actuators and linkages and Stribeck friction (Vermeiren, L., Dequidt, A., Afroun, M., and Guerra, T. M. 2012) applied on prismatic joints appear in this augmented model to provide more realistic simulations.

The dynamics of the actuator writes:

$$\Gamma = M_a \ddot{q}_a + b \dot{q}_a + \Gamma_t + \Gamma_f \tag{27}$$

with  $q_a = [q_{a1}q_{a2}]^T$ ,  $M_a = diag(m_a m_a)Z$ ,  $\Gamma_f = [\Gamma_{f1}\Gamma_{f2}]^T Z$ , the elastic joint model:

$$\Gamma_t = k_t(q_a - q) + b_t(\dot{q}_a - \dot{q}) \tag{28}$$

and the Stribeck friction model of the dry friction:

$$\Gamma_{fi} = \begin{cases} [\Gamma_{fc} + (\Gamma_{fs} - \Gamma_{fc})e^{-(\dot{q}_{ai}/\nu_s)^2}]sign(\dot{q}_{ai}) \\ if |\dot{q}_{ai}| > 0(slip) \\ \min(|\Gamma_i - \Gamma_{ti}|, \Gamma_{fs})sign(\Gamma_i - \Gamma_{ti}) \\ if \dot{q}_{ai} = 0(stick) \end{cases}$$
(29)

where  $m_a$  is the actuator mass,  $k_t$  the stiffness of the joint,  $b_t$  the damping of the joint,  $\Gamma_{fs}$  the static friction force,  $\Gamma_{fc}$  the Coulomb friction force and  $v_s$  the sliding speed coefficient.

The linkage and effector dynamics are:

$$\begin{split} \hat{\Gamma}_t &= \hat{M}(P) \ddot{P} + \hat{N}(P, \dot{P}) \\ \hat{M}(P) &= \begin{pmatrix} m_{L1} + \frac{1}{2}(m - \lambda_1 + \lambda_2) & f_1(P) \\ m_{L2} + \frac{1}{2}(m - \lambda_2 + \lambda_1) & f_2(P) \end{pmatrix} \\ \hat{N}(P, \dot{P}) &= \begin{bmatrix} r_{11} & r_{12} \\ r_{21} & r_{22} \end{bmatrix} \dot{P} + p(y) \\ \begin{cases} r_{11} &= r_{21} \\ r_{12} &= -[(2m_{L1} - 3\lambda_1 - \lambda_2)y^2 + (2m_{L1} - 3\lambda_1 - \lambda_2) \\ C(y)^2 + J_1 + J_2]\dot{y}/(2C(y)^3 \\ r_{22} &= [(2m_{L2} - 3\lambda_2 - \lambda_1)y^2 + (2m_{L2} - 3\lambda_2 - \lambda_1) \\ C(y)^2 + J_1 + J_2]\dot{y}/(2C(y)^3 \\ \text{where the mass linkage } m_{Li} \text{ satisfies: } m_i = m_a + m_{Li}, i = 1, 2. \end{split}$$

Table 1: Parameters model of Biglide parallel robot.

Parameters	Values
Strut length (m) a	0.07
Mass $(kg)$	
m	0.034
m1	0.8040
m2	0.7940
First moment of links (kgm)	
$ms_1$	0.0045
$ms_2$	0.0043
Second moment of links $(kgm^2)$	
$J_1$	$222.643 \times 10^{-4}$
$J_2$	$2.539 \times 10^{-4}$
Gravity acceleration (ms <sup>2</sup> )	
g	9.81
Additional parameter	
for the simulation model Mass $(kg)$	
$\lambda m$	0.816

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