Sensor Reduction for Driver-Automation Shared Steering Control via an Adaptive Authority Allocation Strategy

Tran Anh-Tu Nguyen, Chouki Sentouh, Jean-Christophe Popieul

To cite this version:

Tran Anh-Tu Nguyen, Chouki Sentouh, Jean-Christophe Popieul. Sensor Reduction for Driver-Automation Shared Steering Control via an Adaptive Authority Allocation Strategy. IEEE/ASME Transactions on Mechatronics, 2018, 23 (1), pp.5-16. 10.1109/TMECH.2017.2698216. hal-03428194

HAL Id: hal-03428194
https://uphf.hal.science/hal-03428194
Submitted on 25 Nov 2023

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L’archive ouverte pluridisciplinaire HAL, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d’enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.
Sensor Reduction for Driver-Automation Shared Steering Control via an Adaptive Authority Allocation Strategy

Article in IEEE/ASME Transactions on Mechatronics - February 2018
DOI: 10.1109/TMECH.2017.2698216

CITATIONS
103

READS
530

3 authors, including:

Anh-Tu Nguyen
Université Polytechnique Hauts-de-France
140 PUBLICATIONS  2,084 CITATIONS

Chouki Sentouh
LAMIH UMR CNRS 8201 Hauts-de-France Polytechnic University
114 PUBLICATIONS  2,057 CITATIONS
Sensor Reduction for Driver-Automation Shared Steering Control via an Adaptive Authority Allocation Strategy

Anh-Tu Nguyen, Chouki Sentouh and Jean-Christophe Popieul

Abstract—This paper presents a new shared control method for lane keeping assist (LKA) systems of intelligent vehicles. The proposed method allows the LKA system to effectively share the control authority with a human driver by avoiding or minimizing the conflict situations between these two driving actors. To realize the shared control scheme, the unpredictable driver-automation interaction is explicitly taken into account in the control design via a fictive driver activity variable. This latter is judiciously introduced into the driver-road-vehicle system to represent the driver’s need for assistance in accordance with his/her real-time driving activity. Using Lyapunov stability arguments, Takagi-Sugeno fuzzy model-based design conditions are derived to handle not only the time-varying driver activity variable but also a large variation range of vehicle speed. Both simulation and hardware experiments are presented to demonstrate that the proposed control strategy together with an LMI (linear matrix inequality) design formulation provide an effective tool to deal with the challenging shared steering control issue. In particular, a fuzzy output feedback control scheme is exploited to achieve the shared control goal without at least two important vehicle sensors. These physical sensors are widely employed in previous works to measure the lateral speed and the steering rate for the control design and real-time implementation. The successful results of this idea of sensor-reduction control has an obvious interest from practical viewpoint.

Index Terms—Lane keeping assist system, shared control, human-in-the-loop control, fuzzy model-based control, Lyapunov method, vehicle lateral control.

I. INTRODUCTION

The automobile has been one of the most important products of the twentieth century which has generated an immense industry. However, driving is a dangerous activity and the damages caused by road accidents have serious consequences for individuals and the society. The failure of human drivers’ performance (e.g. inattention, illness, drowsiness) remains one of the most important causes of accidents [1]. This has greatly motivated the research effort from both academic and industrial settings to develop advanced assistance systems to help the driver in various circumstances [2], [3]. In particular, a large body of literature has been recently devoted to the vehicle lateral control, see [4]–[6] and references therein.

From the viewpoint of human-machine interaction, the introduction of a driver steering assistance system into a vehicle can modify the real-time driving activity of the driver and also the risks from the external environment [1]. This naturally leads to the conflict issue between the human driver and the automation in many driving situations. Therefore, the human-automation interaction is considered as the most challenging part in the control design procedure of such assistance systems [2]. Recently, shared control approach has been appeared as a promising solution to deal with this issue [7], [8]. Shared control refers to a control scheme in which there is a combination of a human input and a feedback control function. The control goal is to guarantee that the designed assistance actions do not prevent the human operator to perform some specific tasks that have not been detected by the automation, or even better, the automation should assist him/her to realize these maneuvers. To achieve this goal, an active coordination of control authority between the human driver and the automation is required [9]. Existing works in the framework of the vehicle shared steering control [4], [10] have also shown that the integration of driver’s behaviors into the control loop (via measurements and modeling) contributes to improve the conflict management.

This paper discusses the design of shared controllers for lane keeping assist (LKA) systems of intelligent vehicles. Up to now, shared steering control which can adaptively modify the control authority allocation between the human driver and the LKA system according to the driving conditions still remains open [5], [7]. Based on an $H_2$—preview optimization problem, a shared controller has been presented for only lane keeping task in [4]. A fuzzy-based shared controller for both lane keeping and obstacle avoidance has been also proposed in [10]. It should be stressed that the shared controllers in both [4] and [10] exploit neither the real-time driving activity nor the driving state of human drivers provided by the supervision level to manage the conflict issue. An MPC (model predictive control) framework for shared control has been recently presented in [6], where the control objective of matching the driver’s steering action is conflicting to other ones such as vehicle stability and obstacle avoidance. In particular, the ultimate control authority is always allocated to the automated system, and the driver cannot overrule it. To overcome the above drawbacks, we have proposed to introduce
a fictive variable into the driver-road-vehicle system [5]. This variable, representing the real-time driving information of the human driver, is explicitly considered in the control design to manage effectively the conflict between two driving actors.

Over the years, fuzzy model-based control has been extensively investigated to deal with complex nonlinear systems, see [11]–[13] and references therein. This is mainly due to the following reasons. First, fuzzy systems have universal approximation capability for any smooth nonlinear function. Recently, this outstanding feature has been effectively exploited in [12] (respectively in [14]) to handle the unmodeled dynamics for the design of an adaptive fuzzy backstepping controller of nonlinear systems (respectively nonlinear time-delay systems). Second, based on the use of Takagi-Sugeno (T-S) fuzzy models [11], stability analysis and control design of nonlinear systems can be recast as LMI (linear matrix inequality) optimization problems, which are effectively solved with numerical solvers [15]. Moreover, fuzzy control methods have been successfully applied to numerous real-world applications [5], [16], [17].

Motivated by the above issues, we propose a new fuzzy model-based shared controller for LKA systems. The main features of this paper are summarized as follows. (1) The proposed shared controller is based on the adaptive control authority allocation strategy proposed in [5] to deal with the driver-automation interaction. Hence, this controller can provide an appropriate assistance in accordance with the real-time driving activity of the driver and the driving situations. (2) T-S model-based control is used to handle the time-varying nature of both vehicle speed and the introduced driver activity variable. Note that considering the speed variation into the design procedure is crucial to guarantee not only a good control performance but also a better human-machine coordination under various driving situations [10]. However, this has been mostly neglected in the literature of vehicle coordination under various driving situations [10]. However, this has been mostly neglected in the literature of vehicle lateral control to simplify the design task [4], [6]. (3) In this paper, the measurements of the lateral speed and the steering rate are assumed to be unavailable due to cost reasons of the corresponding sensors. State-feedback control schemes cannot be applied to this situation as most of related works in the control framework of intelligent vehicles [4], [5], [10]. To this end, based on a fuzzy output feedback scheme and an LMI formulation, we propose a sensor reduction control method for LKA systems. By “sensor reduction”, it means that the designed controller can achieve the shared control goal even if the number of feedback sensors is reduced from six to four. (4) Both simulation and experimental results are presented to demonstrate the effectiveness of the proposed shared control methodology. To the best of our knowledge, experimental results of driver-automation shared control with only partial information on the vehicle states have not been reported in the open literature.

This paper extends our preliminary results in [18], provides formal proofs of all technical statements. In particular, experimental results conducted with a human driver and an advanced interactive driving simulator are also included. The paper is organized as follows. Section II presents the modeling of the driver-road-vehicle system. The proposed shared steering control method is discussed in Section III. In Section IV, the development of a T-S fuzzy output feedback controller is presented, and followed by its application to the control design of the studied LKA system. Both numerical simulation and real-time validation results are given in Section V to verify the practical performance of the proposed methodology. Finally, Section VI concludes the paper.

II. DRIVER-VEHICLE MODELING FOR SHARED STEERING CONTROL OF LANE KEEPING ASSIST SYSTEMS

This section presents the modeling of the driver-road-vehicle system used for lateral control purposes. The vehicle parameters and notations are given in Table I.

A. Road-Vehicle Model

Since we focus on the shared steering control, the bicycle model [19] is used here to represent the vehicle lateral dynamics, see Fig. 1. Then, the road-vehicle model integrating the electric power steering system is described by [4], [10]:

\[
\dot{x}_v = Ax_v + B(T_c + T_d) + B_a w
\]

where the vector \(x_v^T = [v_y \quad \psi_L \quad y_L \quad \delta \quad \dot{\delta}]\) is composed of the lateral velocity \(v_y\), the yaw rate \(r\), the heading error \(\psi_L\), the lateral offset \(y_L\) from the road centerline at a look-ahead distance \(s\), the steering angle \(\delta\) and its time derivative \(\dot{\delta}\). For system (1), the driver torque \(T_d\) is designed to manage effectively the human-automation conflict issue. The lateral wind force \(f_w\) and the road curvature \(\rho_r\) are system disturbances, i.e.

\[
w^T = [f_w \quad \rho_r]\ .
\]

The system matrices are given as follows:

\[
A = \begin{bmatrix}
a_{11} & a_{12} & 0 & 0 & b_1 & 0 \\
a_{21} & a_{22} & 0 & 0 & b_2 & 0 \\
0 & 1 & 0 & 0 & 0 & 0 \\
1 & l_s & v_x & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 1 \\
T_{s1} & T_{s2} & 0 & 0 & T_{s3} & T_{s4}
\end{bmatrix},
B_w = \begin{bmatrix}
e_1 & 0 \\
e_2 & 0 \\
0 & -v_x \\
0 & 0 \\
0 & 0 \\
0 & 0
\end{bmatrix},
B = \begin{bmatrix}
0 & 0 & 0 & 0 & 0 & \rho_r^T
\end{bmatrix}^T,
\]

where

\[
a_{11} = -2(C_r + C_f), \quad a_{12} = \frac{2(l_c C_r - l_f C_f)}{M v_x} - v_x, \\
a_{21} = \frac{2(l_c C_r - l_f C_f)}{I_z v_x}, \quad a_{22} = -2(I_r^2 C_r + I_s^2 C_f), \\
T_{s1} = \frac{2K_p C_f \eta_l}{I_s R_s^2 v_x}, \quad T_{s2} = \frac{2K_p C_f \eta_l}{I_s R_s^2 v_x}, \quad \rho = \frac{1}{I_s R_s}, \\
T_{s3} = \frac{2K_p C_f \eta_l}{I_s R_s^2 v_x}, \quad T_{s4} = -\frac{B_s}{I_s}, \quad b_1 = \frac{2C_f}{M}, \\
b_2 = \frac{2l_c C_f}{I_z}, \quad e_1 = \frac{1}{M}, \quad e_2 = \frac{l_w}{I_z}.
\]
TABLE I

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>M</td>
<td>Total mass of the vehicle</td>
<td>2002 [kg]</td>
</tr>
<tr>
<td>l_f</td>
<td>Distance from GC to front axe</td>
<td>1.3 [m]</td>
</tr>
<tr>
<td>l_r</td>
<td>Distance from GC to rear axe</td>
<td>1.6 [m]</td>
</tr>
<tr>
<td>l_w</td>
<td>Distance from GC to wind impact point</td>
<td>0.4 [m]</td>
</tr>
<tr>
<td>l_o</td>
<td>Look-ahead distance</td>
<td>5 [m]</td>
</tr>
<tr>
<td>η_t</td>
<td>Tire length contact</td>
<td>0.13 [m]</td>
</tr>
<tr>
<td>I_v</td>
<td>Vehicle yaw moment of inertia</td>
<td>2800 [kgm²]</td>
</tr>
<tr>
<td>I_s</td>
<td>Steering system moment of inertia</td>
<td>0.05 [kgm²]</td>
</tr>
<tr>
<td>R_s</td>
<td>Steering gear ratio</td>
<td>16 [-]</td>
</tr>
<tr>
<td>B_s</td>
<td>Steering system damping</td>
<td>5.73 [-]</td>
</tr>
<tr>
<td>C_f</td>
<td>Front cornering stiffness</td>
<td>57000 [N/rad]</td>
</tr>
<tr>
<td>C_r</td>
<td>Rear cornering stiffness</td>
<td>59000 [N/rad]</td>
</tr>
</tbody>
</table>

Fig. 1. Lateral vehicle behavior modeling.

B. Driver-in-the-Loop Vehicle Model

For the driving task, the driver is guided on the road by looking at the so-called near point and far point [20]. These two specific points are respectively characterized by two visual angles θ_{near} and θ_{far}. Note that the driving control process of the driver can be divided into two parts: compensatory (represented by G_c = K_{d1}θ_{near}) and anticipatory (represented by G_a = K_{d2}θ_{far}), which may be executed in parallel [21]. Then, the driver torque can be expressed as

\[ T_d = G_c + G_a = K_{d1}θ_{near} + K_{d2}θ_{far} \]  

where the gains K_{d1} and K_{d2} characterizing the driver's style are identified from real-time data. The expressions of two visual angles are given as follows [21]:

\[ \theta_{near} = \frac{y_L}{v_x T_p} + \psi_L, \quad \theta_{far} = \theta_1 v_y + \theta_2 r + \theta_3 \delta_d \]  

\[ \theta_1 = \tau_{a1} a_{21}, \quad \theta_2 = \tau_a + \tau_2 a_{22}, \quad \theta_3 = \tau_3 a_{23}, \quad \delta_d = \delta R_s \]  

where \( T_p \) is the preview time and \( \tau_a \) represents the anticipatory time of the driver. From (2)-(3), the expression of the driver torque can be rewritten in the form

\[ T_d = T_{d1} v_y + T_{d2} r + K_{d1} \psi_L + T_{d3} y_L + T_{d4} \delta \]  

with \( T_{d1} = K_{d1} \theta_1 \rho, \quad T_{d2} = K_{d2} \theta_2 \rho, \quad T_{d3} = \frac{\rho K_{d3}}{v_x T_p}, \quad \text{and} \quad T_{d4} = \rho K_{d3} R_s. \) From (1) and (4), the driver-in-the-loop vehicle model can be represented as

\[ \dot{x}_v = A_v x_v + BT_c + B_w w \]  

where

\[ A_v = \begin{bmatrix} a_{11} & a_{12} & 0 & 0 & b_1 & 0 \\ a_{21} & a_{22} & 0 & 0 & b_2 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & l_s & v_x & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \]

and

\[ \dot{T}_{s1} = T_{s2} + T_{d1}, \quad \dot{T}_{s2} = T_{s3} + T_{d2}, \quad \dot{T}_{s3} = T_{s4} + T_{d4}. \]

Based on (5), we propose in the next section a new driver-road-vehicle model to consider explicitly the real-time driving activity of the human driver in the control design procedure.

III. ADAPTIVE AUTHORITY ALLOCATION FOR DRIVER-AUTOMATION SHARED CONTROL DESIGN

This paper proposes an adaptive shared control strategy for LKA systems that can help the human driver in various driving circumstances. In [9], the driver’s need for assistance according to his/her driving workload and performance has been investigated. This study points out that the level of assistance should be designed to relieve the driver in overload and underload conditions, see Fig. 2. Moreover, to manage effectively the driver-automation conflict, the driver should always remain in the control loop and she/he should receive a continuous feedback from the automation [7]. The proposed shared control strategy follows these guidelines to deal with the human-machine interaction involved in the design procedure. To this end, the assistance torque \( T_c \) is modulated in accordance with the real-time driving activity of the driver

\[ T_c = \mu(\theta_d)u \]  

where the fictive torque \( u \) will be designed and the normalized variable \( \theta_d \) represents the driver’s real-time driving activity as discussed later. Remark that the weighting function \( \mu(\theta_d) \) in (6) allows for a continuous assistance from the LKA system. Inspired by the generalized Bell-shape function, the weighting function \( \mu(\theta_d) \) takes the following form:

\[ \mu(\theta_d) = \frac{1}{1 + \left( \frac{\theta_d - \omega_3}{\omega_1} \right) / \omega_2 + \mu_{\min}} \]  

where \( \omega_1 = 0.355, \omega_2 = -2, \omega_3 = 0.5 \) and \( \mu_{\min} = 0.1. \)

Remark 1. The parameters of \( \mu(\theta_d) \) in (7) are parameterized such that this can represent the U-shape function characterizing the driver’s need for assistance, see Figs. 2 and 3. Observe from (6) that the maximal level of assistance \( \mu_{\max} = 1 \) corresponds to the case where \( u = T_c \). A deadband of minimal level of assistance is necessary to avoid the driver-automation conflict in cases where the driver is not purposely counter steering, see Fig. 3. This deadband should be sufficiently large, which is ensured here by the generalized Bell shape, to allow for a maximum driver reaction torque in shared control mode [2]. The value \( \mu_{\min} = 0.1 \) is chosen such that \( T_c \) can benefit from a large variation range of \( \mu(\theta_d) \), i.e. the real-time information on the driver’s driving activity can be effectively
exploited by the shared controller. However, an unnecessarily small value of $\mu_{\text{min}}$ could induce the design conservatism.

Fig. 2. U-shape function representing the driver’s need for assistance according to her/his driving workload and performance [9].

By taking into account the driving variable $\theta_d$ into (4), the driver-in-the-loop vehicle model used for the control design can be then deduced from (5)-(6) as follows:

$$\Sigma_v (v_x, \mu(\theta_d)) : \dot{x}_v = A_v x_v + B_u u + B_w w \quad (8)$$

where

$$A_v = \begin{bmatrix} a_{11} & a_{12} & 0 & 0 & b_1 & 0 \\ a_{21} & a_{22} & 0 & b_2 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & l_s & v_x & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \\ \tilde{T}_{d1} & \tilde{T}_{d2} & \tilde{K}_{d1} & \tilde{T}_{d3} & \tilde{T}_{d4} & \tilde{T}_{s4} \end{bmatrix}, \ B_u = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ \tilde{\rho} \end{bmatrix}.$$

For system (8), the real-time driving activity of the driver is also taken into account in the driver model (4) as follows:

$$\tilde{T}_{d1} = T_{s1} + (1 - \mu(\theta_d)) T_{d1}, \quad \tilde{T}_{d2} = T_{s2} + (1 - \mu(\theta_d)) T_{d2},$$
$$\tilde{T}_{d3} = (1 - \mu(\theta_d)) T_{d3}, \quad \tilde{T}_{d4} = T_{s3} + (1 - \mu(\theta_d)) T_{d4},$$
$$\tilde{K}_{d1} = (1 - \mu(\theta_d)) K_{d1}/I_s, \quad \tilde{\rho} = \mu(\theta_d) \rho.$$

For the proposed method, the driver activity variable $\theta_d$ depends on two factors: (i) the measured driver torque $T_d$, and (ii) the driver state variable ($0 \leq DS \leq 1$) provided by the driver monitoring system [5], [22]:

$$\theta_d = 1 - e^{-(\sigma_1 T_d)^{\sigma_2 DS^{\sigma_3}}} \quad (9)$$

where the tuning parameters are given by $\sigma_1 = 2$ and $\sigma_2 = \sigma_3 = 3$. The normalized driver torque is defined as $T_{dN} = \frac{T_d}{T_{d\text{max}}}$ where $T_{d\text{max}}$ is the maximal torque can be delivered by the driver. The parameter $\sigma_1$ is used together with $T_{dN}$ to represent the involvement level of the driver in the driving tasks whereas the parameters $\sigma_2$ and $\sigma_3$ represent the degree of influence of the driver torque and the driver state on the driver activity variable $\theta_d$. These three parameters are tuned such that the information from the supervision level ($T_d$ and $DS$) are judiciously exploited in (9) to represent the real-time driving activity of the driver. Fig. 4 shows that when the driver torque and/or the driver state remain(s) small (which means that the driver activity is not significant), the corresponding values of the normalized variable $\theta_d$ are small and a high level of assistance is required. When the driver is highly involved in his/her driving tasks, i.e. $\theta_d$ tends to 1 (for example in the case where the driver needs to realize a difficult driving task), an important level of assistance from the LKA system is also required to help him/her. With a constant driver torque (respectively driver state), the driving activity of the driver increases according to the value of the driver state $DS$ (respectively driver torque).

For the driver-road-vehicle system (8), six physical sensors are necessary to measure all vehicle states for a full state-feedback control scheme. However, since the measurements of the lateral velocity $v_y$ and the steering angle rate $\dot{\delta}$ are unavailable, such a control scheme cannot be applied here. In addition, the dynamics of system (8) depends strongly on the vehicle speed $v_x$ and the driver activity variable $\theta_d$ which are time-varying. In next section, we develop a sensor reduction method based on T-S fuzzy output feedback control and LMI formulation to overcome these practical issues.

IV. SENSOR REDUCTION VIA FUZZY DYNAMIC OUTPUT FEEDBACK CONTROL

Sensor reduction based control approach can be formulated as an output feedback control problem [23]. To reduce the number of feedback sensors, we first derive the conditions for stability arguments and LMI techniques. Then, the application of theoretical results to the shared lateral control is presented.

A. Closed-Loop Description of Takagi-Sugeno Fuzzy Systems

Consider the following T-S fuzzy model [11]:

$$\dot{x} = \sum_{i=1}^{r} \eta_i(\theta) (A_i x + B_i^u u + B_i^w w)$$
$$z = \sum_{i=1}^{r} \eta_i(\theta) (C_i^z x + D_i^{zu} u + D_i^{zw} w)$$
$$y = \sum_{i=1}^{r} \eta_i(\theta) (C_i^y x + D_i^{yu} u + D_i^{yw} w) \quad (10)$$
where $x \in \mathbb{R}^{n_x}$ is the system state, $u \in \mathbb{R}^{n_u}$ is the control input, $w \in \mathbb{R}^{n_w}$ is the system disturbance, $y \in \mathbb{R}^{n_y}$ is the measured output, $z \in \mathbb{R}^{n_z}$ is the performance output, and $\theta \in \mathbb{R}^{k}$ is the vector of measured premise variables. The matrices of appropriate dimensions $A_i$, $B_i^w$, $B_i^r$, $C_i^r$, $D_i^{zw}$, $D_i^{yu}$, $C_i^y$ and $D_i^{yw}$, $i \in \{1, \ldots, r\}$, represent the set of $r$ local linear subsystems. The scalar membership functions $\eta_i(\theta)$ satisfy the following convex sum property:

$$\sum_{i=1}^{r} \eta_i(\theta) = 1, \quad \eta_i(\theta) \geq 0, \quad i \in \{1, \ldots, r\}.$$  

The fuzzy output feedback controller is constructed based on the following dynamic parallel distributed compensation law:

$$\dot{x}_c = \sum_{i=1}^{r} \sum_{j=1}^{r} \eta_i(\theta) \eta_j(\theta) A_{ij} x_c + \sum_{i=1}^{r} \eta_i(\theta) B_i^r y$$

$$u_c = \sum_{i=1}^{r} \eta_i(\theta) C_i^r x_c + D_c y, \quad x_c(0) = 0$$  

where $x_c \in \mathbb{R}^{n_x}$, $u_c \in \mathbb{R}^{n_u}$ are respectively the state and the output of the controller. Let us define $x_{cl} = [x^\top \ x_c^\top]^\top$, from (10) and (11) the closed-loop system is given as follows:

$$\dot{x}_{cl} = \sum_{i=1}^{r} \sum_{j=1}^{r} \eta_i(\theta) \eta_j(\theta) (A_{i} x_{cl} + B_{ij}^w w)$$

$$z = \sum_{i=1}^{r} \sum_{j=1}^{r} \eta_i(\theta) \eta_j(\theta) (C_{ij} x_{cl} + D_{ij}^w w)$$  

where

$$A_{ij} = \begin{bmatrix} A_i + B_i^w D_i^y C_j^r & B_i^w C_j^r \\ B_i^r C_j^r & A_i^r \end{bmatrix}$$

$$B_{ij}^w = \begin{bmatrix} B_i^w + B_i^r D_i^w D_j^{yw} \\ B_i^r D_j^{yw} \end{bmatrix}$$

$$C_{ij} = \begin{bmatrix} C_i^r + D_i^{zw} D_j^y C_j^r \\ D_i^{yu} C_j^y \end{bmatrix}$$

$$D_{ij}^w = \begin{bmatrix} D_i^{zw} + D_i^{yu} D_j^{yw} \\ D_i^{yw} \end{bmatrix}$$

The output of the fuzzy controller (11) is given by

$$u_c = \sum_{i=1}^{r} \eta_i(\theta) (K_i x_{cl} + K_i^w w)$$

where $K_i = [D_i C_i^y \ C_i^r]$ and $K_i^w = D_i^r D_i^{yw}$.

Notation. The following notations are introduced for brevity. For a matrix $X$, $X^\top$ denotes its transpose. For any square matrix $X$, $X > 0$ means $X$ is symmetric positive definite and $\text{He}(X) = X + X^\top$. $I$ denotes the identity matrix of appropriate dimension. $(\ast)$ stands for matrix blocks that can be deduced by symmetry. $\text{diag}(\cdot)$ denotes a block diagonal matrix formed by the blocks given in the parenthesis. For brevity, the scalar function $\eta_i(\theta)$ is denoted by $\eta_i, i \in \{1, \ldots, r\}$.

B. Fuzzy Model-Based Output Feedback Control Design

For real-world applications, it is important to consider not only the stability but also other performance specifications. Hereafter, a constructive LMI-based design for stability, decay rate and $\mathcal{H}_\infty$ performance of the closed-loop system (12) is derived.

Definition 1. The T-S system (12) is stable with a decay rate $\alpha > 0$ if there exists a positive definite function

$$\mathcal{V}(x_{cl}) = x_{cl}^\top P x_{cl}, \quad P > 0$$  

such that

$$\dot{\mathcal{V}}(x_{cl}) < -2\alpha \mathcal{V}(x_{cl})$$  

for any solution $x_{cl}$ of (12). The speed of response of the closed-loop system is related to the decay rate [11].

Definition 2. If the T-S system (12) is stable and satisfies

$$\int_0^\infty z(t)^\top z(t) dt < \gamma^2 \int_0^\infty w(t)^\top w(t) dt$$  

for $x_{cl}(0) = 0$. Then, the $\mathcal{H}_\infty$ norm of (12) is said to be less than $\gamma$. The constraint (15) can be interpreted as a disturbance rejection performance. This constraint is also useful to enforce robust stability [24].

The following theorem allows for the design of a dynamic output feedback controller (11) satisfying the closed-loop properties defined in (14) and (15).

Theorem 1. Given a T-S fuzzy system (10) and a positive scalar $\alpha$. Assume there exist positive definite matrices $P_{11} \in \mathbb{R}^{n_x \times n_x}$, $X_{11} \in \mathbb{R}^{n_u \times n_x}$, matrices $\hat{A}_{ij} \in \mathbb{R}^{n_x \times n_x}$, $\hat{B}_i \in \mathbb{R}^{n_x \times n_y}$, $\hat{C}_i \in \mathbb{R}^{n_y \times n_x}$ and $\hat{D} \in \mathbb{R}^{n_y \times n_y}$ for $i, j \in \{1, \ldots, r\}$, and a positive scalar $\gamma > 0$ such that

$$X_{11} I = P_{11}$$

$$\sum_{i=1}^{r} \sum_{j=1}^{r} \eta_i \eta_j \Xi_{ij} < 0$$  

where the quantity $\Xi_{ij}$ is defined as

$$\Xi_{ij} = \begin{bmatrix} \Xi_{ij}^{[1]} & \Xi_{ij}^{[2]} & \Xi_{ij}^{[3]} & \Xi_{ij}^{[4]} \\ \ast & \Xi_{ij}^{[2]} & \Xi_{ij}^{[3]} & \Xi_{ij}^{[4]} \\ \ast & \ast & -\gamma I & \Xi_{ij}^{[3]} \\ \ast & \ast & \ast & -\gamma I \end{bmatrix}$$

and $\Xi_{ij}^{[1]} = \text{He}(A_i X_{11} + B_i^r \hat{C}_j + \alpha X_{11})$, $\Xi_{ij}^{[2]} = A_i + B_i^w \hat{D} C_j^r + \hat{A}_{ij}^r + 2\alpha I$, $\Xi_{ij}^{[3]} = B_i^w \hat{D} D_j^{yw} + B_i^w$, $\Xi_{ij}^{[4]} =$...
\[ He(P_{i1}A_i + \hat{B}_i C^y_j + \alpha P_{i1}), \Xi_{ij}^{[23]} = P_{i1}^w B_i + \hat{B}_i D^w_j, \Xi_{ij}^{[24]} = (C_i^T X_{11} + D_{iu}^w \hat{C}_j)^T, \Xi_{ij}^{[34]} = (D^w_j + D_{iu}^w D^w_j) \]\n
Let \( P_{i2} \) and \( X_{12} \) be two nonsingular matrices such that
\[ P_{i1} X_{11} + P_{i2} X_{12}^T = I. \] (19)

Then, the fuzzy output feedback controller (11) with the feedback gains defined by
\[ D^c = \hat{D} \] (20)
\[ C_i^c = (\hat{C}_i - D^c C^y_i) X_{11}^T \]
\[ B_i^c = P_{i2}^{-1} (\hat{B}_i - P_{i1} B_i^w D^c) \]
\[ A_i^c = P_{i2}^{-1} (\hat{A}_{ij} - P_{i1} (\hat{A}_i + B_i^w D^c C^y_j) X_{11} - P_{i2} B_i^c C_i^c X_{12}^T) X_{12}^{-T} \]

for \( i, j \in \{1, \ldots, r\} \), solves the control problem stated above.

Proof. Conditions (16) and (19) imply the existence of two matrices \( P_{i2} \) and \( X_{12} \) such that the following block matrices:
\[ \Pi = \begin{bmatrix} P_{i1} & P_{i2} \\ P_{i2}^T & P_{i2} \end{bmatrix}, \quad X = \begin{bmatrix} X_{11} & X_{12} \\ X_{12}^T & X_{22} \end{bmatrix} \]
are positive definite [24]. Note that the same properties guarantee the existence of two nonsingular matrices \( P_{i2} \) and \( X_{12} \). The T-S fuzzy system (12) is stable while satisfying the decay rate (14) and the \( H_\infty \) performance (15) if
\[ \dot{\gamma}(x_c) + 1 \gamma^T z - \gamma w^T w < -2\alpha \gamma(x_c) \] (21)

Using the explicit expressions of the closed-loop system (12) and the Lyapunov function (13), (21) can be rewritten as
\[ \xi^T \Gamma \xi < 0 \] (22)

where \( \xi = [x_c^T \ w^T] \) and
\[ \Gamma = \sum_{i=1}^r \sum_{j=1}^r \eta_{ij} \begin{bmatrix} He(P_{i1} A_i + \alpha P_{i1}) & * \\ P_{i2} B_i P_{i1} & -\gamma I \end{bmatrix} + \frac{1}{\gamma} \Lambda_{ij}^T \Lambda_{ij} \]
with \( \Lambda_{ij} = [C_{ij} D_{wij}] \). It is clear that (22) is verified if \( \Gamma < 0 \). By Schur complement lemma [15], this latter is equivalent to
\[ \sum_{i=1}^r \sum_{j=1}^r \eta_{ij} \begin{bmatrix} He(P_{i1} A_i + \alpha P_{i1}) & * \\ P_{i2} B_i P_{i1} & -\gamma I \end{bmatrix} + \frac{1}{\gamma} \Lambda_{ij}^T \Lambda_{ij} < 0 \] (23)

Let us define \( \Pi = \begin{bmatrix} X_{11} & I \\ X_{12}^T & 0 \end{bmatrix} \). Pre- and postmultiplying (23) with \( \Pi^T, \Pi \) and its transpose leads to
\[ \sum_{i=1}^r \sum_{j=1}^r \eta_{ij} \begin{bmatrix} \Pi^T \Phi_{ij} \Pi & * \\ D_{wij}^T & -\gamma I \end{bmatrix} + \frac{1}{\gamma} \Lambda_{ij}^T \Lambda_{ij} < 0 \] (24)

where \( \Phi_{ij} = A_{ij}^T I + P_{i1} A_i + \alpha P_{i1}. \) The convexification procedure of (24) can be performed with the following definitions:
\[ \hat{A}_{ij} = P_{i2} A_i X_{12} + P_{i1} (A_i + B_i^w D^c C^y_j) X_{11} + P_{i2} B_i C_i^c X_{11} + P_{i1} B_i^w C_i^c X_{12} \]
\[ \hat{B}_i = P_{i2} B_i X_{12} + P_{i1} B_i^w D^c \]
\[ \hat{C}_i = C_i^T X_{12} + D^c C_i^c X_{11} \]
\[ \hat{D} = D^c \]

for \( i, j \in \{1, \ldots, r\} \). Using (25), the following identities can be straightforwardly obtained:
\[ \Pi^T P_{i1} A_i \Pi = \begin{bmatrix} A_i X_{11} + B_i^w \hat{C}_j & A_i + B_i^w \hat{D} C^y_j \\ \hat{A}_{ij} & P_{i1} A_i + \hat{B}_i C^y_j \end{bmatrix}, \]
\[ \Pi^T P_{i2} B_i \Pi = \begin{bmatrix} B_i^w \hat{D} D^w_j + B_i^w \hat{D} D^w_j & B_i^w \hat{D} D^w_j + B_i^w \hat{D} D^w_j \end{bmatrix}, \]
\[ \Pi^T P_{i2} \Pi = \begin{bmatrix} X_{11} & I \\ I & P_{i1} \end{bmatrix} \]

Replacing the explicit expressions of \( \Pi^T P_{i1} A_i \Pi, \Pi^T P_{i2} B_i \Pi \) and \( C_i^c \Pi \) into (24) leads directly to (17). Moreover, the feedback gains (20) can be easily recovered from the change of variable (25). Thus, the proof of Theorem 1 can be concluded.

**Remark 2.** Condition (17) is represented in the form of a parameterized linear matrix inequality. Here, the relaxation result in [25] is applied to convert (17) into the following finite set of LMIs:
\[ \Xi_{ii} < 0, \quad i \in \{1, \ldots, r\} \]
\[ 2 \frac{r-1}{r} \Xi_{ii} + \Xi_{ij} + \Xi_{ji} < 0, \quad i, j \in \{1, \ldots, r\}, \quad i < j \] (26)

**Remark 3.** The equation (19) admits infinite solutions of \( P_{i2} \) and \( X_{12} \) parameterizing an infinite number of controllers (11). However, these controllers satisfy the same decay rate and \( H_\infty \) performance since \( P_{i2} \) and \( X_{12} \) are not explicitly involved in the LMIs of Theorem 1. Therefore, the choice of \( P_{i2} \) and \( X_{12} \) satisfying (19) is irrelevant for the proposed control method. One possible way to determine these nonsingular matrices is based on the well-known singular value decomposition in conjunction with the Cholesky factorization, namely
\[ P_{i2} X_{12} = I - P_{i1} X_{11} = USV^T = UR^T RU^T. \] (27)

Then, one has clearly that \( P_{i2} = UR^T \) and \( X_{12} = VR^T \).

The following theorem summarizes the discussions given in Remarks 2, 3 and provides LMI-based design conditions for the considered control problem.

**Theorem 2.** Given a T-S fuzzy system (10) and a positive scalar \( \alpha \). If there exist positive definite matrices \( P_{i1} \in \mathbb{R}^{n_s \times n_s}, X_{11} \in \mathbb{R}^{n_s \times n_s}, \) matrices \( \hat{A}_{ij} \in \mathbb{R}^{n_s \times n_s}, \hat{B}_i \in \mathbb{R}^{n_s \times n_s}, \hat{C}_i \in \mathbb{R}^{n_s \times n_s}, \) and \( D \in \mathbb{R}^{n_s \times n_s} \) for \( i, j \in \{1, \ldots, r\} \) and a positive scalar \( \gamma \) such that the LMIs (16) and (26) are verified where the quantity \( \Xi_{ij} \) is defined in (18). Then, the T-S fuzzy system (10) is stabilized by the output feedback controller (11) with an \( H_\infty \) norm less than \( \gamma \). The controller gains are given in (20) while two nonsingular matrices \( P_{i2} \) and \( X_{12} \) can be computed from (27).

**Remark 4.** Theorem 2 provides a systematic method to design a fuzzy output feedback controller (11). The design procedure is formulated as a convex optimization so that the feedback gains (20) can be effectively computed with available numerical toolboxes, e.g. YALMIP toolbox [26].

In what follows, the application of Theorem 2 to the shared control design of the studied LKA system is highlighted.
C. Design of Shared Controller for LKA Systems

Since the lateral speed \( v_y \) and the steering rate \( \dot{\delta} \) are assumed to be unmeasurable, the output equation of the T-S fuzzy model (10) for the driver-vehicle system is given by

\[
y = \sum_{i=1}^{r} \eta_i(\theta) \left( C_i^y x + D_i^{yw} w \right)
\]

where

\[
C_i^y = C = \begin{bmatrix}
0 & 1 & 0 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 1 & 0
\end{bmatrix}, \quad D_i^{yw} = 0.
\]

To take into account the \( \mathcal{H}_\infty \) performance (15), the controlled output is defined as follows:

\[
z = W \begin{bmatrix}
\dot{a}_y \\
\dot{\theta}_r \\
\dot{\theta}_{near} \\
\dot{\theta}_{far} \\
\dot{\delta}
\end{bmatrix}^{T}
\]

\[
W = \text{diag}(q_{a_y}, q_{\dot{\psi}_r}, q_{\dot{\theta}_{near}}, q_{\dot{\theta}_{far}}, q_\delta)
\]

where \( q_{a_y}, q_{\dot{\psi}_r}, q_{\dot{\theta}_{near}}, q_{\dot{\theta}_{far}}, \) and \( q_\delta \) are the weighting coefficients. Note that the lane keeping performance is represented by the near and far visual angles in (28) which allow respectively for the consideration of the driver’s compensatory and anticipatory behaviors, see (3). The driver’s comfort is represented by the lateral acceleration \( a_y \) and the relative yaw rate \( \dot{\psi}_r \) as

\[
a_y = v_x r_r, \quad \dot{\psi}_r = r - v_x \rho_r.
\]

The steering wheel rate \( \dot{\delta} \) is introduced in (28) to guarantee a desired comfort for the steering correction. Then, the performance output matrices in (10) of (8) are given by

\[
C_i^z = W \begin{bmatrix}
v_x & 0 & 0 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 & 0 & 0 \\
\theta_1 & \theta_2 & 0 & 0 & \theta_3 & 0 \\
0 & 0 & 0 & 0 & 1 & 0
\end{bmatrix}, \quad D_i^{zu} = 0
\]

\[
D_i^{zw} = \begin{bmatrix}
0 & 0 & 0 & 0 & 0 & 0 \\
0 & -v_x & 0 & 0 & 0 & 0
\end{bmatrix}^{T}, \quad i \in \{1, \ldots, r\}
\]

Note that the system matrices in (8) and (29) depend nonlinearly on the vehicle speed (i.e. \( v_x \) and \( 1/v_x \)), and the driver variable \( \mu(\theta_d) \) which are measured and bounded

\[
v_{\min} \leq v_x \leq v_{\max}, \quad \mu_{\min} \leq \mu(\theta_d) \leq \mu_{\max},
\]

where \( v_{\min} = 9 \), \( v_{\max} = 30 \), \( \mu_{\min} = 0.1 \) and \( \mu_{\max} = 1 \).

The T-S fuzzy modeling of the driver-in-the-loop vehicle system could be done with the natural choice of premise variables \( \theta = [v_x, 1/v_x, \mu(\theta_d)]^{T} \in \mathbb{R}^3 \). Using the sector nonlinearity approach [11], this choice leads to an exact T-S fuzzy representation (10) with \( r_s = 2^3 = 8 \) linear subsystems. However, this T-S fuzzy driver-vehicle model would be too costly in terms of numerical computation for control purposes, and especially for real-time implementation. Here, the strong relationship between \( v_x \) and \( 1/v_x \) is exploited through the first order Taylor’s approximation to reduce significantly the numerical complexity of the proposed control method

\[
\frac{1}{v_x} = \frac{1}{v_0} + \frac{1}{v_1} \Delta_x, \quad v_x \cong v_0 \left( 1 - \frac{v_0}{v_1} \Delta_x \right)
\]

where \( \Delta_{\min} \leq \Delta_x \leq \Delta_{\max}, \) \( \Delta_{\min} = -1 \) and \( \Delta_{\max} = 1 \). The new measured time-varying parameter \( \Delta_x \) is used to describe the variation of \( v_x \) between its lower and upper bounds. The two constants \( v_0 \) and \( v_1 \) are given by

\[
v_0 = \frac{2v_{\min} v_{\max}}{v_{\min} + v_{\max}}, \quad v_1 = \frac{2v_{\min} v_{\max}}{v_{\min} - v_{\max}}.
\]

Replacing (30) into (8), the premise variables can be now defined as \( \theta = [\Delta_x, \mu(\theta_d)]^{T} \in \mathbb{R}^2 \). By the sector nonlinearity approach, the corresponding T-S fuzzy driver-vehicle model has only \( r = 2^2 = 4 \) linear subsystems

\[
\Sigma_{r1}(\Delta_{\min}, \mu_{\min}), \quad \Sigma_{r2}(\Delta_{\min}, \mu_{\max}), \quad \Sigma_{r3}(\Delta_{\max}, \mu_{\min}), \quad \Sigma_{r4}(\Delta_{\max}, \mu_{\max}).
\]

The corresponding membership functions are defined as

\[
\eta_1 = \Omega_{\Delta 1} \mu_1, \quad \eta_2 = \Omega_{\Delta 1} \mu_2, \quad \eta_3 = \Omega_{\Delta 2} \mu_1, \quad \eta_4 = \Omega_{\Delta 2} \mu_2,
\]

where

\[
\Omega_{\Delta 1} = \frac{\Delta_{\max} - \Delta_x}{\Delta_{\max} - \Delta_{\min}}, \quad \Omega_{\Delta 2} = \frac{\Delta_x - \Delta_{\min}}{\Delta_{\max} - \Delta_{\min}},
\]

\[
\Omega_{\mu 1} = \frac{\mu_{\max} - \mu(\theta_d)}{\mu_{\max} - \mu_{\min}}, \quad \Omega_{\mu 2} = \frac{\mu(\theta_d) - \mu_{\min}}{\mu_{\max} - \mu_{\min}}.
\]

Theorem 2 can be now applied to the T-S fuzzy driver-in-the-loop vehicle model to design the output feedback controller (11) for shared control purposes.

V. SIMULATION AND HARDWARE EXPERIMENTS

This section presents the results of a series of both simulation and hardware experiments to demonstrate the practical performance of the proposed shared control method.

A. Numerical Simulation

All simulations are conducted using Matlab/Simulink platform with the nonlinear vehicle model given in [10]. The sensorimotor driver model proposed in [27] is used to simulate the behaviors of a human driver. The test track is depicted in Fig. 5 (left), which consists of a straight road section followed by four curves with different radius \( R_1 = 50 \) [m], \( R_2 = 33 \) [m], \( R_3 = 25 \) [m] and \( R_4 = 20 \) [m]. Fig. 5 (right) shows the road curvature and the vehicle speed corresponding to the considered test track.

![Fig. 5. Vehicle trajectory (left), vehicle speed and road curvature (right).]
1) Scenario 1 [Lane Keeping Control Performance]: This test is composed of three phases. For the first phase (from $t = 0$ s to $t = 15$ s), the vehicle is fully controlled by the designed shared steering controller ($T_d = 0$), see Fig. 6 (a). Observe in Fig. 6 (b) that $\mu(\theta_d) = 1$ during this period which means that the maximal level of assistance is required to perform the driving task. In the second phase (from $t = 15$ s to $t = 50$ s), both the driver and the shared controller are involved in the driving process. During this maneuver, the weighting parameter $\mu(\theta_d)$ decreases progressively to 0.4 (respectively 0.2) for the second (respectively third) curve taking. This means that only a small level of assistance is required to assist the driver in these situations. The third phase begins at the end of the third curve where the driver torque $T_d$ decreases quickly to zero and the parameter $\mu(\theta_d)$ tends to 1. This means that the shared controller has a full control authority during this phase as indicated in Fig. 6 (from $t = 50$ s to $t = 70$ s).

![Fig. 6. Lane keeping maneuver: (a) steering torques in shared control, (b) control authority allocation in accordance with the driver’s real-time activity.](image)

Fig. 6. Lane keeping maneuver: (a) steering torques in shared control, (b) control authority allocation in accordance with the driver’s real-time activity.

The comparison of the near visual angle $\theta_{near}$ obtained with two above cases is presented in Fig. 7 (a). Observe that small values of $\theta_{near}$ are achieved with Case 1 where its maximal value does not exceed $\pm 10^\circ$. In addition, the shared controller allows the driver model to perform better the taking of curves without overshoot of $\theta_{far}$, see Fig. 7 (b). The overshoot of $\theta_{far}$ means that the vehicle has an under-steering behavior. Fig. 7 (c) shows the comparison of the lateral deviation errors, remark that this error in Case 1 has an opposite sign compared to the road curvature, which means that the vehicle slightly cuts the bends to minimize $\theta_{far}$. This result points out the interest of considering the driver’s behaviors in the control design of the shared lane keeping driving process.

![Fig. 7. Control performance comparison between shared controller and full automatic controller.](image)

Fig. 7. Control performance comparison between shared controller and full automatic controller.

B. Experimental Validation

1) SHERPA Interactive Dynamic Driving Simulator: This advanced simulator is in the form of a Peugeot 206 vehicle fixed on a Stewart platform, the whole is positioned in front of five flat panel displays providing a visual field of 240°, see Fig. 8. Based on a distributed computing architecture, this complex simulator is structured around a SCANeR network connecting fifteen PC-type workstations. The whole software of the SHERPA simulator is developed with RTMaps environment composed by several modules which are in charge of different tasks: perception, planning, driver monitoring, human-machine interface. This driving simulator is equipped with a Continental driver monitoring system which indicates the information on the driver’s drowsiness/distraction and provides the driver state variable $DS$ used in (9). In what follows, all experiments have been carried out with the SHERPA simulator and a human driver.

Note that for the control design, the driver-road-vehicle model (8) has been first identified and then experimentally validated with the data collected from the SHERPA simulator, see also [5], [10]. For illustrations, Fig. 9 shows the validation...
results obtained with the database of a test track, located in Satory, 20 km west of Paris, France. We can see that this real-world track consists of several curved sections including tight bends, and the vehicle speed corresponding to the validation test is strongly time-varying as indicated in Figs. 9 (a) and (b). Observe that the responses of (8) are highly close to the behaviors of the SHERPA simulator even when the driver purposely performs a zigzag driving pattern on a straight road section to produce high-frequency control inputs, see Figs. 9 (c), (d), (e) and (f). Therefore, the driver-road-vehicle model (8) can be exploited for the design of shared lateral controllers.

Fig. 9. Experimental validation of the driver-road-vehicle model obtained with the SHERPA simulator and the digital database of the Satory test track.

2) **Scenario 3 [Wind Disturbance Rejection]**: Assume that the vehicle is on a straight road with \( v_x = 15 \) [m/s] and subject to an important wind force \( f_w = 1000 \) [N], see Fig. 10 (a). This wind force generates a yaw moment disturbance which can be felt by the driver through the steering wheel. The disturbance rejection performance of the proposed control method is examined for three following cases:

- Case 1: full automatic control \((T_d = 0)\),
- Case 2: manual control \((T_c = 0)\),
- Case 3: driver-automation shared control.

Observe in Figs. 10 (b) and (c) that for all three cases, the required torques for disturbance rejection are similar and the lateral accelerations remain small. In particular, for Case 3 the assistance torque \(T_c\) is in accordance with the driver’s need for assistance (represented by \(\mu(\theta_d)\)) to help the driver. Thus, both driving actors jointly control the vehicle (i.e. their torques have the same sign) and the driver provides a smaller effort than that of Case 2 to perform the same task, see Fig. 10 (d).

Fig. 10 shows the comparison of the vehicle responses obtained with three above cases. As can be seen, the closed-loop behaviors of these cases are quite close. However, with the proposed shared controller (Case 3), the driver only needs to provide about half amount of the required torque for disturbance rejection, see Fig. 10 (d). This is particularly useful not only to improve the driving comfort but also to ensure the security in cases where the driver (for some reasons such as illness, inattention, etc.) cannot provide enough effort for the driving task. Observe also in Fig. 11 that the wind disturbance is effectively rejected for all three cases since all tracking performance variables remain small during the test.

To further point out the interest of the \(H_\infty\) performance in terms of disturbance rejection, let us compare the control performance obtained with full automatic control \((T_d = 0)\) for two cases: with and without consideration of (15) in the control design presented in Theorem 2. As expected, Fig. 12 shows a clear improvement (i.e. smaller tracking errors under the effect of the wind disturbance) when the \(H_\infty\) performance is explicitly taken into account in the synthesis procedure.

3) **Scenario 4 [Driver Monitoring for Shared Control]**: This test aims to show the crucial role of the driver monitoring in the proposed shared control method. To this end, the lane keeping is performed in shared control mode (i.e. both the human driver and the proposed shared controller are involved in the driving task) over a section of the Satory test track, see Fig. 13 (a). The corresponding vehicle speed is depicted in Fig. 13 (e). This test scenario can be divided into two phases. For the first phase (from \( t = 0 \)s to \( t = 45 \)s), the driver is assumed to be fully aware of the driving situation with \(DS = 1\) as indicated in Fig. 13 (c). As expected, both driving actors jointly
control the vehicle in this phase to perform different curve takings with different levels of assistance (according to the curve radius), see Figs. 13 (b) and (d). These experimental results also confirm those presented in Fig. 6 and indicate the usefulness of the simulation studies.

The second phase (from $t = 45s$ to $t = 75s$) corresponds to a lane keeping on a straight lane with the assumption that the driver is distracted ($DS = 0$), see Fig. 13 (c). For this, the driver did not watch the road (to simulate the distraction) while applying some torque on the steering wheel. As indicated in Fig. 13 (d), the maximal level of assistance is now required to realize the driving task with a “distracted” driver. As a consequence, the LKA system counteracts the driver’s actions (i.e., their respective torques are in the opposite sign) to avoid the lane departure, see Fig. 13 (b). We can also observe in Figs. 13 (f), (g), and (h) that during the driving Scenario 4, the vehicle is maintained in the lane despite the driver’s distraction in the second phase and the tracking performance variables remain small over the whole driving test.

The above numerical and experimental results point out the effectiveness of the new shared control method under various driving circumstances despite the unavailability of two important vehicle sensors for lateral speed and steering rate.

**VI. CONCLUDING REMARKS**

An adaptive control authority allocation approach has been proposed to deal with the shared steering control between a human driver and a LKA system. To this end, a measured variable representing the real-time driving activity of the driver has been judiciously introduced into the driver-road-vehicle system. As a result, the designed actions of the LKA system can be computed in accordance with the driver’s behaviors and the challenging driver-automation interaction is effectively managed. T-S fuzzy model-based control has been used to handle the time-varying nature of the driver activity variable and the vehicle speed. In particular, the proposed solution is cost-effective in the sense that a fuzzy output feedback control scheme is exploited to reduce two important vehicle sensors.
These latter have been intensively used in previous works for the control design and real-time implementation although they are not always available in commercial vehicles. The effectiveness of the proposed control methodology has been clearly demonstrated through both numerical and hardware experiments with different driving situations. Future works focus on the intensive human-factor experiments with a large panel of drivers and different real-world driving conditions to further evaluate the new shared control methodology for the LKA systems of intelligent vehicles.

REFERENCES


Anh-Tu Nguyen received Engineering and MSc degrees in 2009 from Grenoble Institute of Technology, France, and PhD degree in Automatic Control in 2013 from the University of Valenciennes, France. After working a short period in 2010 at the French Institute of Petroleum, Dr. Nguyen began his doctoral program at the CNRS laboratory LAMH in collaboration with VALEO Group. He was a postdoctoral researcher at the CNRS laboratory LS2N. His research interests include robust control, constrained control systems, human-machine shared control for intelligent vehicles.

Chouki Sentouh received the MSc degree from the University of Versailles, France in 2003 and his PhD degree in Automatic Control from the University of Evry, France, in 2007. Dr. Sentouh was a postdoctoral researcher at the CNRS laboratory IKCCyN, France, from 2007 to 2009. Since 2009, he is an Associate Professor at the University of Valenciennes in LAMH-UMR CNRS 8201. His research fields include automotive control, driver assistance systems with driver interaction, human driver modeling and cooperation in intelligent transportation systems, shared control for assistance systems.

Jean-Christophe Popieul is Professor in Automatic Control at the University of Valenciennes in LAMH-UMR CNRS 8201. Since 1994 his main area of interest is in Vehicle Dynamics and Control. He is a member of several scientific boards, including ANR, PREEDIT, i-Trans competitiveness cluster, IRT Raisenum. He is also the head of several Interactive Simulation Platforms of the LAMH: SHERPA driving simulator, PSCHITT-Rail train/tramway simulator and PSCHITT-PMR wheelchair simulator.

View publication stats